

AS and A level Mathematics Practice Paper – Coordinate geometry – Mark scheme

Question	Scheme	Marks
1	<p>Mid-point of PQ is $(4, 3)$</p> <p>$PQ: m = \frac{0-6}{9-(-1)}, \left(= -\frac{3}{5} \right)$</p> <p>Gradient perpendicular to $PQ = -\frac{1}{m} (= \frac{5}{3})$</p> <p>$y-3 = \frac{5}{3}(x-4)$</p> <p>$5x-3y-11=0$ or $3y-5x+11=0$ or multiples e.g. $10x-6y-22=0$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>
		(5 marks)
2(a)	<p>Method 1</p> <p>$gradient = \frac{y_1 - y_2}{x_1 - x_2} = \frac{2 - (-4)}{-1 - 7}, = -\frac{3}{4}$</p> <p>$y - 2 = -\frac{3}{4}(x + 1)$ or $y + 4 = -\frac{3}{4}(x - 7)$ or $y = \text{their}' - \frac{3}{4}x + c$</p> <p>$\Rightarrow \pm(4y + 3x - 5) = 0$</p> <p>Method 3: Substitute $x = -1, y = 2$ and $x = 7, y = -4$ into $ax + by + c = 0$</p> <p>$-a + 2b + c = 0$ and $7a - 4b + c = 0$</p> <p>Solve to obtain $a = 3, b = 4$ and $c = -5$ or multiple of these numbers</p>	<p>M1 A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1 A1</p>
		(4)
2(b)	<p>Attempts</p> <p>$gradient LM \times gradient MN = -1$ so</p> <p>$-\frac{3}{4} \times \frac{p+4}{16-7} = -1$ or $\frac{p+4}{16-7} = \frac{4}{3}$</p> <p>$p+4 = \frac{9 \times 4}{3} \Rightarrow p = \dots, p = 8$ So $y =, y = 8$</p>	<p>M1</p> <p>M1 A1</p>
		(3)
2(c)	<p>Either $(y =) p + 6$ or $2 + p + 4$</p> <p>$(y =) 14$</p> <p>Or use 2 perpendicular line equations through L and N and solve for y</p>	<p>M1</p> <p>A1</p>
		(2)
		(9 marks)

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3(a)	Gradient of $l_1 = \frac{4}{5}$ oe Point $P = (5, 6)$ $-\frac{5}{4} = \frac{y - "6"}{x - 5}$ or $y - "6" = -\frac{5}{4}(x - 5)$ or $"6" = -\frac{5}{4}(5) + c \Rightarrow c = ...$ $5x + 4y - 49 = 0$	B1 B1 M1 A1 (4)
3(b)	$y = 0 \Rightarrow 5x + 4(0) - 49 = 0 \Rightarrow x = ...$ or $y = 0 \Rightarrow 5(0) = 4x + 10 \Rightarrow x = ...$ $y = 0 \Rightarrow 5x + 4(0) - 49 = 0 \Rightarrow x = ...$ and $y = 0 \Rightarrow 5(0) = 4x + 10 \Rightarrow x = ...$ <u>Method 1:</u> $\frac{1}{2} ST \times "6"$ $\frac{1}{2} \times ('9.8' - '2.5') \times '6' = ...$ <u>Method 2:</u> $\frac{1}{2} SP \times PT$ $\frac{1}{2} \times \sqrt{('5' - '2.5')^2 + ('6')^2} \times \sqrt{('9.8' - '5')^2 + ('6')^2} = ...$ $= \frac{1}{2} \times \frac{3\sqrt{41}}{2} \times \frac{6\sqrt{41}}{5}$ <u>Method 3:</u> 2 Triangles $\frac{1}{2} \times (5 + '2.5') \times '6' + \frac{1}{2} \times ('9.8' - 5) \times '6' = ...$ <u>Method 4:</u> Shoelace method $\frac{1}{2} \begin{vmatrix} 5 & 9.8 & -2.5 & 5 \\ 6 & 0 & 0 & 6 \end{vmatrix} = \frac{1}{2} (0 + 0 - 15) - (58.8 + 0 + 0) = \frac{1}{2} -73.8 = ...$ <u>Method 5:</u> Trapezium + 2 triangles $\frac{1}{2} \times ('2.5') \times '2' + \frac{1}{2} ("2" + "6") \times 5 + \frac{1}{2} \times ("9.8" - 5) \times '6' = ...$ $= 36.9$	M1 M1 ddM1 A1 (4)
		(8 marks)

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4(a)	(a) $2x + 3y = 26 \Rightarrow 3y = 26 \pm 2x$ and attempt to find m from $y = mx + c$ $(\Rightarrow y = \frac{26}{3} - \frac{2}{3}x)$ so gradient = $-\frac{2}{3}$ Gradient of perpendicular = $\frac{-1}{\text{their gradient}} (= \frac{3}{2})$ Line goes through (0,0) so $y = \frac{3}{2}x$	M1 A1 M1 A1 (4)
4(b)	(b) Solves their $y = \frac{3}{2}x$ with their $2x + 3y = 26$ to form equation in x or in y Solves their equation in x or in y to obtain $x = \text{or } y =$ $x = 4$ or any equivalent e.g. $156/39$ or $y = 6$ o.a.e $B = (0, \frac{26}{3})$ used or stated in (b) Area = $\frac{1}{2} \times "4" \times \frac{"26"}{3}$ $= \frac{52}{3}$ (oe with integer numerator and denominator)	M1 dM1 A1 B1 dM1 A1 (6)
		(10 marks)

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5(a)	$L_1: 4y + 3 = 2x \Rightarrow y = \frac{1}{2}x - \frac{3}{4}$; $A(p, 4)$ lies on L_1 . $\{p =\} 9\frac{1}{2}$ or $\frac{19}{2}$ or 9.5	B1 (1)
5(b)	$\{4y + 3 = 2x\} \Rightarrow y = \frac{2x - 3}{4} \Rightarrow m(L_1) = \frac{1}{2}$ or $\frac{2}{4}$ So $m(L_2) = -2$ $L_2: y - 4 = -2(x - 2)$ $L_2: 2x + y - 8 = 0$ or $L_2: 2x + 1y - 8 = 0$	M1 A1 B1ft M1 A1 (5)
5(c)	$\{L_1 = L_2 \Rightarrow\} 4(8 - 2x) + 3 = 2x$ or $-2x + 8 = \frac{1}{2}x - \frac{3}{4}$ $x = 3.5, y = 1$	M1 A1 A1 cso (3)
5(d)	$CD^2 = ("3.5" - 2)^2 + ("1" - 4)^2$ $CD = \sqrt{("3.5" - 2)^2 + ("1" - 4)^2}$ $= \sqrt{1.5^2 + 3^2} = 1.5 \sqrt{1^2 + 2^2} = 1.5 \sqrt{5}$ or $\frac{3}{2} \sqrt{5}$ (*)	“M1” A1 ft A1 cso (3)
5(e)	Area = triangle ABC + triangle ABE $= \frac{1}{2} \times \frac{3}{2} \sqrt{5} \times \sqrt{80} + \frac{1}{2} \times 3 \sqrt{5} \times \sqrt{80}$ $= \frac{3}{4} \sqrt{5} \times 4 \sqrt{5} + \frac{3}{2} \sqrt{5} \times 4 \sqrt{5}$ $= \frac{3}{4}(20) + \frac{3}{2}(20)$ $= 45$	Finding the area of any triangle. M1 B1 A1 (3)
		(15 marks)

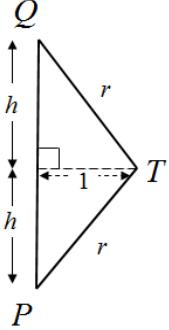
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Question	Scheme	Marks
6(a)	Gradient of l_1 is $\frac{7-2}{3-0} \left(= \frac{5}{3} \right)$ $m(l_2) = -1 \div \text{their } \frac{5}{3}$ $y - 7 = " - \frac{3}{5} "(x - 3)$ or $y = " - \frac{3}{5} "x + c, 7 = " - \frac{3}{5} "(3) + c \Rightarrow c = \frac{44}{5}$ $3x + 5y - 44 = 0$	B1 M1 M1A1ft A1 (5)
6(b)	When $y = 0 \ x = \frac{44}{3}$	M1 A1 (2)
6(c)	Correct attempt at finding the area of any one of the triangles or one of the trapezia. A correct numerical expression for the area of one triangle or one trapezium for their coordinates . Combines the correct areas together correctly Correct numerical expression for the area of $ORQP$ Correct exact area e.g. $54\frac{1}{3}$, $\frac{163}{3}$, $\frac{326}{6}$, $54.\dot{3}$ or any exact equivalent	M1 A1ft dM1 A1 A1 (5)
		(12 marks)
7	The equation of the circle is $(x+1)^2 + (y-7)^2 = (r^2)$ The radius of the circle is $\sqrt{(-1)^2 + 7^2} = \sqrt{50}$ or $5\sqrt{2}$ or $r^2 = 50$ So $(x+1)^2 + (y-7)^2 = 50$ or equivalent	M1 A1 M1 A1
		(4 marks)

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8(a)	$\{PQ =\} \sqrt{(7-10)^2 + (8-13)^2}$ or $\sqrt{(10-7)^2 + (13-8)^2}$ $\{PQ\} = \sqrt{34}$	M1 A1 (2)
8(b)	$(x-7)^2 + (y-8)^2 = 34$ (or $(\sqrt{34})^2$)	M1 A1 oe (2)
8(c)	{Gradient of radius} $= \frac{13-8}{10-7}$ or $\frac{5}{3}$ Gradient of tangent $= -\frac{1}{m} \left(= -\frac{3}{5} \right)$ $y - 13 = -\frac{3}{5}(x - 10)$ $3x + 5y - 95 = 0$	B1 M1 M1 A1 (4)
		(8 marks)
9(a)	$x^2 + y^2 + 4x - 2y - 11 = 0$ $\{(x+2)^2 - 4 + (y-1)^2 - 1 - 11 = 0\}$ Centre is $(-2, 1)$.	M1 M1 A1 cao (2)
9(b)	$(x+2)^2 + (y-1)^2 = 11 + 1 + 4$ So $r = \sqrt{11+1+4} \Rightarrow r = 4$ $r = \sqrt{11 \pm "1" \pm "4"}$ 4 or $\sqrt{16}$ (Award A0 for ± 4).	M1 A1 (2)
9(c)	When $x = 0$, $y^2 - 2y - 11 = 0$ $y = \frac{2 \pm \sqrt{(-2)^2 - 4(1)(-11)}}{2(1)} \quad \left\{ = \frac{2 \pm \sqrt{48}}{2} \right\}$ So, $y = 1 \pm 2\sqrt{3}$	Putting $x = 0$ in C or their C. $y^2 - 2y - 11 = 0$ or $(y-1)^2 = 12$, etc Attempt to use formula or a method of completing the square in order to find $y = \dots$ $1 \pm 2\sqrt{3}$ A1 cao cso (4)
		(8 marks)

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10(a)	$x^2 + y^2 - 10x + 6y + 30 = 0$ Uses any appropriate method to find the coordinates of the centre, e.g. achieves $\underline{(x \pm 5)^2} + \underline{(y \pm 3)^2} = \dots$. Accept $(\pm 5, \pm 3)$ as indication of this. Centre is $(5, -3)$.	M1 A1 (2)
10(b)	Way 1 Uses $\underline{(x \pm "5")^2} - "5^2" + \underline{(y \pm "3")^2} - "3^2" + 30 = 0$ to give $r = \sqrt{"25" + "9" - 30}$ or $r^2 = "25" + "9" - 30$ (not $30 - 25 - 9$) $r = 2$ Way 2 Using $\sqrt{g^2 + f^2 - c}$ from $x^2 + y^2 + 2gx + 2fy + c = 0$ (Needs formula stated or correct working) $r = 2$	M1 A1cao M1 A1 (2)
10(c)	Way 1 Use $x = 4$ in <i>an</i> equation of circle and obtain equation in y only e.g. $(4-5)^2 + (y+3)^2 = 4$ or $4^2 + y^2 - 10 \times 4 + 6y + 30 = 0$ Solve their quadratic in y and obtain two solutions for y e.g. $(y+3)^2 = 3$ or $y^2 + 6y + 6 = 0$ so $y = -3 \pm \sqrt{3}$ Way 2  <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> Divide triangle PTQ and use Pythagoras with $"r"^2 - ("5" - 4)^2 = h^2$ Find h and evaluate $-3 \pm h$ May recognise $(1, \sqrt{3}, 2)$ triangle </div> <div style="width: 45%;"> $"r"^2 - ("5" - 4)^2 = h^2$ $Find h and evaluate -3 \pm h$ $May recognise (1, \sqrt{3}, 2) triangle$ </div> </div> <p style="text-align: center;">So $y = -3 \pm \sqrt{3}$</p>	M1 dM1 A1 M1 dM1 A1 (3)
		(7 marks)

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11(a)	<p style="text-align: center;">Mark (a) and (b) together</p> $OQ^2 = (6\sqrt{5})^2 + 4^2 \text{ or } OQ = \sqrt{(6\sqrt{5})^2 + 4^2} \quad \{= 14\}$ $y_Q = \sqrt{14^2 - 11^2}$ $= \sqrt{75} \text{ or } 5\sqrt{3}$	M1 dM1 A1 cso (3)
11(b)	$(x - 11)^2 + (y - 5\sqrt{3})^2 = 16$	M1A1 (2)
		(5 marks)
12(a)	$A\left(\frac{-9+15}{2}, \frac{8-10}{2}\right) = A(3, -1)$	M1A1 (2)
12(b)	$(-9 - 3)^2 + (8 + 1)^2 \text{ or } \sqrt{(-9 - 3)^2 + (8 + 1)^2}$ or $(15 - 3)^2 + (-10 + 1)^2 \text{ or } \sqrt{(15 - 3)^2 + (-10 + 1)^2}$ Uses Pythagoras correctly in order to find the radius . Must clearly be identified as the radius and may be implied by their circle equation. Or $(15 + 9)^2 + (-10 - 8)^2 \text{ or } \sqrt{(15 + 9)^2 + (-10 - 8)^2}$ Uses Pythagoras correctly in order to find the diameter . Must clearly be identified as the diameter and may be implied by their circle equation. This mark can be implied by just 30 clearly seen as the diameter or 15 clearly seen as the radius (may be seen or implied in their circle equation) Allow this mark if there is a correct statement involving the radius or the diameter but must be seen in (b) $(x - 3)^2 + (y + 1)^2 = 225 \quad (\text{or } (15)^2)$ $(x - 3)^2 + (y + 1)^2 = 225$	M1 M1 A1 (3)
12(c)	Distance $= \sqrt{15^2 - 10^2}$ $\{= \sqrt{125}\} = 5\sqrt{5}$	M1 A1 (2)
12(d)	$\sin(A\hat{R}Q) = \frac{20}{30} \text{ or } A\hat{R}Q = 90 - \cos^{-1}\left(\frac{10}{15}\right)$ $A\hat{R}Q = 41.8103\dots$ awrt 41.8	M1 A1 (2)
		(9 marks)

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	Source paper	Question number	New spec references	Question description	New AOs
1	C1 2011	3	3.1	Straight lines	1.1b
2	C1 2017	8	3.1	Straight-line graph (perpendicular gradients)	1.1b, 2.1, 2.4 and 3.1a
3	C1 June 2014R	7	3.1	Equation of straight line and condition for perpendicularity	1.1b, 2.1, 2.2a, 3.1a
4	C1 2014	9	3.1	Coordinate geometry, perpendicularity	1.1b, 3.1a
5	C1 2012	9	3.1, 2.4	Straight lines, Indices and surds, Simultaneous equations	1.1a, 1.1b, 2.1, 2.2a, 3.1a
6	C1 2016	10	3.1	Lines, perpendicular	1.1b, 2.1, 2.4, ,3.1a
7	C2 Jan 2012	Q2	3.2	Circles	1.1b
8	C2 2016	3	3.1, 3.2	Circles	1.1b
9	C2 2011	Q4	2.3, 3.2	Circles	1.1b, 3.1a
10	C2 2017	5	3.2	Circles	1.1a, 1.1b, 3.1a
11	C2 2014	9	3.2	Circles	1.1b, 3.1a
12	C2 June 2014R	10	3.2	Circles	1.1b, 2.2a. 3.1a