Functions and graphs 2F



y = 3f(x) + 2. Vertical translation of +2.



b y = f(x-2). Horizontal translation of +2.



y = f(x-2) - 5.Vertical translation of -5.



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1 c y = f(x+1)

Horizontal translation of -1.



Vertical stretch, scale factor $\frac{1}{2}$



 $\mathbf{d} \quad y = \mathbf{f}(2x)$

Horizontal stretch, scale factor $\frac{1}{2}$



y = -f(2x)Reflection in the *x*-axis. (or Vertical stretch, scale factor -1).



e y = |f(x)|. Reflect, in the *x*-axis, the parts of the graph that lie below the *x*-axis.



1 f y = f(-x). Reflection in the *y*-axis.

 $y = \left| \mathbf{f} \left(-x \right) \right|.$

Reflect, in the *x*-axis, the parts of the graph that lie below the *x*-axis.



2 a y=f(x-2)Horizontal translation of +2



y = 3f(x-2)Vertical stretch, scale factor 3.



b $y = f\left(\frac{1}{2}x\right)$

Horizontal stretch, scale factor 2.



2 b (continued)



 $\mathbf{c} \quad y = -\mathbf{f}(x)$

Reflection in the *x*-axis.

(Or vertical stretch, scale factor -1).



y = -f(x) + 4Vertical translation of +4.



d y = f(x+1)Horizontal translation of -1.



y = -2f(x+1)Reflection in the *x*-axis, and vertical stretch, scale factor 2.



2 e y = f(|x|) can be written

$$y = \begin{cases} f(x), \ x \ge 0\\ f(-x), \ x < 0 \end{cases}$$

y = f(-x) is a reflection of

y = f(x) in the y-axis.

Hence, y = f(|x|) is the following:

$$y = 2f\left(\left|x\right|\right)$$

Vertical stretch, scale factor 2.





Asymptotes: *x* = 2, *y* = -1 *A*: (0, 2)

3 a y = 3f(x)Vertical stretch, scale factor 3.



y = 3f(x) - 1Vertical translation of -1.

3 b y = f(x+2)





y = f(x+2) + 4

Vertical translation of +4.



Asymptotes: *x* = 0, *y* = 4 *A*: (-2, 5)

c y = f(2x)Horizontal stretch, scale factor $\frac{1}{2}$



y = -f(2x). Reflection in the *x*-axis.



A: (0, -1)

3 d y = f(|x|) can be written

$$y = \begin{cases} f(x), \ x \ge 0\\ f(-x), \ x < 0 \end{cases}$$

- y = f(-x) is a reflection of
- y = f(x) in the y-axis.

Hence, y = f(|x|) is the following:



Asymptotes are x = -2, x = 2 and y = 0. A: (0, 1)

4 a



b i
$$(2+4, -9 \times 2) = (6, -18)$$

ii
$$(2 \times \frac{1}{2}, -9) = (1, -9)$$

iii $(2, -9 \times -1) = (2, 9)$

c
$$y = g(|x|)$$
 can be written

$$y = \begin{cases} g(x) = (x-2)^2 - 9, \ x \ge 0\\ g(-x) = (x+2)^2 - 9, \ x < 0 \end{cases}$$

y = g(-x) is a reflection of

y = g(x) in the y-axis.

Hence,
$$y = g(|x|)$$
 is the following:



5 a $y = 2\sin x$ is a vertical stretch of $y = \sin x$ by a scale factor 2.



b minimum $A(-90^\circ, -2)$ and maximum $B(90^\circ, 2)$

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5 c i h(x-90) is a horizontal translation of +90° h(x-90)+1 is a vertical translation of +1.



ii $h\left(\frac{1}{2}x\right)$ is a horizontal stretch scale factor 2 $\frac{1}{4}h\left(\frac{1}{2}x\right)$ is a vertical stretch

scale factor
$$\frac{1}{4}$$

$$\begin{array}{c} y \\ \frac{1}{2} \\ O(0, 0) \\ \hline -360 \\ A(-180, -\frac{1}{2}) \\ \hline \\ A(-180, -\frac{1}{2}) \\ \hline \\ \end{array} \begin{array}{c} y \\ B(180, \frac{1}{2}) \\ \hline \\ 180 \\ 360 \\ \end{array} \begin{array}{c} y \\ y = \frac{1}{4}h(\frac{1}{2}x) \\ \hline \\ 180 \\ 360 \\ \end{array}$$

iii h(-x) is a reflection in the y-axis |h(-x)| causes the part of the graph below the x-axis to be reflected in the x-axis. $\frac{1}{2}|h(-x)|$ is a vertical stretch scale factor $\frac{1}{2}$ $A(-90, 1) \begin{array}{c} y \\ 1 \\ - \end{array} \qquad B(90, 1) \\ y = \frac{1}{2}|h(-x)|$



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