AP Calculus Formulae Sheet

	Shanos	
Area of Triangle	Shapes ¹ / _a x base x height	
Area of Parallelogram	base x height	
Area of Trapezoid	$\frac{1}{2}$ (sum of parallel sides) x height	
Circumference & Area: Circle Cuboid Surface area	$c = 2\pi r, A = \pi r^2$ $SA = 2xy + 2xz + 2yz$	
	where $x, y, and z$ are side lengths	
Cuboid Volume	V = xyz where x, y, and z are side lengths	
Cylinder Surface Area	$SA = 2\pi rh + 2\pi r^2$	
Cylinder Volume	Note: Curved part: $2\pi rh$ $V = \pi r^2 h$	
Cone Surface Area	$SA = \pi r l + \pi r^2$	
Cone Volume	Note: Curved part: $\pi r l$, where l is slant length	
Sphere Surface Area	$V = \frac{1}{3}\pi r^2 h$ $SA = 4\pi r^2 \text{ (Hemisphere} = 3\pi r^2 \text{)}$	
Sphere Volume	$v = \frac{4}{3}\pi r^3 \text{ (Hemisphere = } \frac{2}{3}\pi r^3\text{)}$	
Prism Volume	V = Area of cross section x height	
Pyramid Volume	$V = \frac{1}{3} \times base \ area \times h$	
	Indices	
Multiplication	$x^{a} \times x^{b} = x^{a+b}$ $(cx^{a}y^{b})^{d} = c^{d}x^{ad}y^{bd}$	
Division	$(cx^{a}y^{b})^{a} = c^{a}x^{ad}y^{bd}$ $x^{a} \div x^{b} = \frac{x^{a}}{x^{b}} = x^{a-b}$	
Negative Powers	1	
Fractions	$\chi^{-n} = \frac{1}{\chi^n}$ $(\chi)^n \chi^n (\chi)^{-n} \chi^n$	
	$\left(\frac{x}{y}\right)^n = \frac{x^n}{y^n} \text{ and } \left(\frac{x}{y}\right)^{-n} = \frac{y^n}{x^n}$	
Rational Powers	$a^{\frac{n}{m}} = (\sqrt[m]{a})^n$ Binomial	
Binomial Theorem:	$(a+b)^n$	
integer powers	$=a^{n}+\binom{n}{1}a^{n-1}b+\cdots+\binom{n}{r}a^{n-r}b^{r}++b^{n}$	
Binomial Coefficient	$\binom{n}{r} = nc_r = \frac{n!}{(n-r)! r!}$	
	Geometry	
Straight Line: Equation	• Slope intercept form: $y = mx + c$	
(gradient means slope) ∥ same slope, ⊥ "flip fraction,	 General form: ax + by + d = 0 Point slope form: y - y₁ = m(x - x₁) 	
change sign" which means slopes × to make −1)		
Straight Line: Gradient	$m = \frac{y_{2} - y_{1}}{x_{2} - x_{2}}$	
Distance between	$\frac{m - x_{2-}x_{1}}{\sqrt{(x_{2-}x_{1})^{2} + (y_{2-}y_{1})^{2}}}$	
$(x_1, y_1), (x_2, y_2)$		
Coordinates of midpoint of	$\left(\frac{x_{1+}x_{2}}{2}, \frac{y_{1+}y_{2}}{2}\right)$	
$(x_1, y_1), (x_2, y_2)$	Quadratics	
Quadratic Function: Solutions	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}, a \neq 0$	
to $ax^2 + bx + c = 0$ Quadratic Function:		
Axis of Symmetry	$f(x) = x^2 + bx + c \Rightarrow x = -\frac{b}{2a}$ $\Delta = b^2 - 4ac$	
Quadratic Function: Discriminant	> 0 (2 real distinct roots)	
	= 0 (2real repeated/double roots) < 0 (no real roots)	
Completing The Square	$a\left(x \pm \frac{b}{2a}\right)^2 + c - \frac{b^2}{4a}$	
$ax^2 \pm bx + c = 0$ Exponentials & Logarithm	$a\left(x \pm \frac{1}{2a}\right) + c - \frac{1}{4a}$ • $c \log_a b \Leftrightarrow \log_a b^c$	
Rules`	• $\log_a b = c \Leftrightarrow a^c = b, a, b, > 0, a \neq 1$	
	• $\log_a b + \log_a c \Leftrightarrow \log_a bc$	
	• $\log_a b - \log_a c \Leftrightarrow \log_a \frac{b}{c}$ • $\log_a b \Leftrightarrow \frac{\log_c b}{c}$	
	 log_a b ⇔ log_c b / log_c a Solving a power of x: log both sides if 2 	
	terms or use substitution if 3 terms	
	 Solving an exponential: In both sides Solving a logarithm: raise e both sides or 	
	write as \log_e as proceed as for \log	
Polynomials, Rational	aling with Inequalities Use number line to put zeros and undefined	
Mod	points and check signs either side	
IVIUU	$ x < a \Longrightarrow -a < x < a$ $ x > a \Longrightarrow x < -a \ OR \ x > a$	
	OR: graph each and then see where one graph lies above (>)/below (<) the other	
	Limits	
Graphically: Can we trace inwards coordinate? If yes, has a limit	from the left and right and still reach the same y	
• •		
Method: Direct substitution, if get a number	or one of the following 4 then done:	
1) $\frac{Any non zero number}{0}$ = undefined	$2) \frac{\pm \infty}{non infinte number} = \pm \infty$	
2) 0 -0	4) Any non infinte number = 0	
3) = 0 1) and 2) just say that there is no li	±∞ mit and 3) and 4) just say limit is zero	
If not, and get $\frac{0}{0}$ or $\frac{\infty}{\omega}$ it is indeterminate form and not an answer. We then either		
 Factorise and cancel 		
 Rationalise and cancel Use a trig identity and cancel 		
 Apply L' Hopital's Rule (differentiate numerator and denominator) and then apply substitution again 		
Other hints:		
If trig and $\rightarrow 0$: use small angle approx. or identity and simplify or squeeze theorem If algebraic and $\rightarrow \infty$: divide by highest power in denominator or memorise that		
	Even powers in numerator and denominator	
 Even powers in n 		
 Even powers in n Bottom heavy y Top Heavy y = 0 	= 0 o (no asymptote)	
$ \begin{array}{ccc} \bullet & & \text{Even powers in n} \\ \bullet & & \text{Bottom heavy } y \\ \bullet & & \text{Top Heavy } y = 0 \\ \text{Note: Watch out for when you hav} \end{array} $	= 0 • (no asymptote) e roots in the denominator.	
• Even powers in n • Bottom heavy y • Top Heavy y = o Note: Watch out for when you haw If all the above has failed use squeen	= 0 o (no asymptote) e roots in the denominator. eze theorem! Continuity	
Even powers in r Bottom heavy y Top Heavy y = o Note: Watch out for when you hav If all the above has failed use squee Graphically: Can we trace the curve	= 0 o (no asymptote) er oots in the denominator. eze theorem! Continuity without taking pen off page? If yes, continuous!	
Even powers in r Bottom heavy y Top Heavy y = o Note: Watch out for when you hav If all the above has failed use squee Graphically: Can we trace the curve	= 0 o (no asymptote) e roots in the denominator. eze theorem! Continuity	

ction is continuous at a point c if f(c) is defined, meaning the function has a value at x=c i.e. when you plug c in the function it returns a value

 $\lim f(x)$ exists i.e, $\lim_{x \to a} f(x) = \lim_{x \to a} f(x)$, meaning the limit

 $\lim f(x) = f(c)$, meaning the value of the function at x=c is equal

exists at x=c (i.e. the two sided limits are equal)

to the value of the limit at x =

2)

3)

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	Trigonometry
Sine Rule	Finding a side: $\frac{a}{\sin A} = \frac{b}{\sin R} = \frac{c}{\sin C}$ Finding an angle: $\frac{\sin A}{\sin A} = \frac{\sin B}{b} = \frac{\sin C}{c}$
Cosine Rule	Finding an angle: $\frac{\sin a}{a} = \frac{\sin b}{b} = \frac{\sin c}{c}$ inding a side: $a^2 = b^2 + c^2 - 2bc \cos A$
	Finding an angle: $A = \cos^{-1} \left(\frac{b^2 + c^2 - a^2}{2bc} \right)$
Area of Triangle	$\frac{1}{2}absinC$
Degrees to radians and vice versa	D to R: $\times \frac{\pi}{180}$ R to D: $\times \frac{180}{\pi}$
Length of an arc	$\frac{\theta}{360} \times 2\pi r$ (degrees) or $r\theta$ (radians) $\frac{\theta}{360} \times \pi r^2$ (degrees) or $\frac{1}{2}r^2\theta$ (radians)
Area of a Sector	$\frac{\partial b}{\partial f} \times \pi r^2$ (degrees) or $\frac{1}{2}r^2\theta$ (radians)
Small Angle Approximations	$\sin \theta \approx \theta$, $\cos \theta \approx 1 - \frac{\theta^2}{2}$, $\tan \theta \approx \theta$
Pythagorean identity 1	$\sin^2 x + \cos^2 x = 1$
Pythagorean identity 2	$1 + tan^2x = sec^2x.$
Pythagorean identity 3	$1 + cot^2x = cosec^2x$
Cofunction	$\cos x = \sin(90 - x)$
Identity of tan x	$\sin x = \cos (90 - x)$ $\tan x = \frac{\sin x}{1 + \cos x}$
Reciprocal	$\tan x = \frac{\sin x}{\cos x}$ $\sec x = \frac{1}{\cos x}, \csc x = \frac{1}{\sin x}, \cot x = \frac{1}{\tan x}$
Double Angle	$\sin 2x = 2\sin x \cos x$
	$cos2x = cos^2x - sin^2x$ $= 2 cos^2x - 1 \Rightarrow cos^2x = \frac{cos^2x + 1}{2}$ $= 1 - 2 sin^2\theta \Rightarrow sin^2x = \frac{1 - cos^2x}{2}$
	$\tan 2x = \frac{2\tan x}{1 - \tan^2 x}$
Half Angle	$\frac{1 - \tan^2 x}{\sin \frac{x}{2}} = \pm \sqrt{\frac{1 - \cos x}{2}} \qquad \cos \frac{x}{2} = \pm \sqrt{\frac{\cos x + 1}{2}}$
Compound Angle	$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
	$cos(A \pm B) = cosAcosB \mp sinAsinB$
	$tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$
Special Angles	A 70 AT 40
openar ruigies	Sin 0 2 3 4
	210 0 1 2 3 4 COS 4 3 2 1 0
5 /0.11	
Even/Odd	$\sin(-x) = -\sin x, \cos(-x) = \cos x,$
	$\tan(-x) = -\tan x$
Average value of function for [a h]	Averages
Average value of function f on [a,b] Average rate of function of f on	$\frac{\frac{1}{b-a} \int_a^b f(x) dx}{\frac{f(b)-f(a)}{b-a}}$
[a,b]	
Instantaneous rate at $x = c$ (Note: at a point, not an interval)	f'(c)
(Functions
Inverse	Replace $f(x)$ with y , swap $x \& y$, solve for y
Composite	fg(x) means plug $g(x)$ into $f(x)$
Transformations: af(bx + c) + d	a=vertical stretch sf a , b=horizontal stretch sf $\frac{1}{b}$ c=translation c units x direction,
"anything in a bracket does the	d=translation d units in y direction
opposite"	f(-x)=reflc in y $axis$, $-f(x)$ =reflc in y $axis$
Inverse Odd/Even	Replace $f(x)$ with y , swap $x \& y$, solve for y Even: $f(-x) = f(x)$, odd: $f(-x) = -f(x)$
Periodic	f(x+p) = f(x) where p is the period
Basic Domain	Fractions $= : x \in \mathbb{R}, x \neq \text{value(s)}$ where denom $= 0$
"the x values allowed"	Roots: $$: Solve for part under root to be ≥ 0
(see table below for domain and range for all common functions in	Exponentials $e^{}: x \in \mathbb{R}$ (power can be anything, no restriction on it)
more detail)	Logarithms $\ln ()$: Solve for argument to be > 0
Linear: $y = mx + c$ Domain: $x \in \mathbb{R}$	Rational: $\frac{ax+b}{cx+d} + e$
Range: y∈ ℝ	Domain: $x \in \mathbb{R}$, $x \neq -\frac{d}{c}$ (Hint:denom \neq 0)
Quadratic: $y = \pm a(bx + c)^2 + d$ Domain: $x \in \mathbb{R}$	Range: $y \in \mathbb{R}$, $y \neq \frac{a}{c} + e$
Range: $y \ge d$ if min, $y \le d$ if max Exponential: $y = ae^{bx+c} + d$	Asymptotes: $x = -\frac{d}{c}$, $y = \frac{a}{c} + e$ Note: often a and or e are zero
Exponential: $y = ae^{bx+c} + d$	Trigonometry: $y = asin(bx + c) + d$
Domain: x∈ ℝ (Hint: power of exp c be anything, so no restriction)	y = acos(bx + c) a
Range: $y > d$ if $a > 0$, $y < d$ if $a < 0$	0 Domain: $x \in \mathbb{R}$ Range: $-a + d \le y \le a + d$
(Hint: exp can't be zero) Logarithm: $y = aln(bx + c)+d$	Note: If asked to find values of a,b,c,d
Domain: $x > -\frac{c}{b}$ (Hint: $\ln \operatorname{can't}$ tak	$a = \text{amplitude} = \frac{\max y - \min y}{2}$ $b = \frac{2\pi}{360} = \frac{360}{360}$
a neg number so $bx + c > 0$) Range: $y \in \mathbb{R}$	$b = \frac{2\pi}{period}$ or $\frac{360}{period}$ $d = principal axis= \frac{max y + min y}{2}$
Asymptote: $x = -\frac{c}{b}$	$a = \text{principal axis} = \frac{c}{2}$ $c = \text{phase shift (plug in point to find after}$
Root: $a\sqrt{bx+c}+d$: Domain: $x \ge -\frac{c}{b}$ (Hint: under root	finding a, b and d) Trigonometry: $y = atan(bx + c) + d$
must be positive so b $x + c \ge 0$)	Domain: $x \in \mathbb{R}, x \neq \frac{\pi}{2} + n\pi$
Range: $y \ge d$ if $a > 0$ and $y \le d$ if	Range: $-\infty \le y \le \infty$
a<0 Modulus $a bx+c +d$:	Inverse trig: $y = sin^{-1}x$ Domain: $-1 \le x \le 1$
Domain: $x \in \mathbb{R}$	Range: $-\frac{\pi}{2} \le x \le \frac{\pi}{2}$
Range: $y \ge d$ if $a > 0$ and $y \le d$ if $a < 0$	Inverse trig: $y = cos^{-1}x$ Domain: $-1 \le x \le 1$
Note: Definition of $ x = \begin{cases} x, x \ge 0 \\ -x, x < 0 \end{cases}$	Range: $0 \le x \le \pi$
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,	Range: $-\frac{\pi}{2} < x < \frac{\pi}{2}$
	harder rational functions

Graphing harder rational functions

- Vertical asymptotes set denominator =0 and solve Horizontal asymptotes: Find $\lim_{x \to \infty} f(x)$
- Easiest method: Can just use the fact that even powers y = coefficients of ratio of
- Easiest inertious. Lail pus tase the left in die even jowers y = cole in terms of ratio of highest powers, Bottom heavy y = 0, Top Heavy $y = \infty$ (no asymptote) Slant: only exists if top heavy. Divide and quotient part is slant asymptote Intercepts : set x = 0, find y and vice versa check the behaviour each side of vertical asymptote x = a: $\lim_{x \to a^+} f(x)$ and $\lim_{x \to a^+} f(x)$. We want to know whether y tends to tend to $+\infty$ $or -\infty$
- Easiest Method: Can just try a value just less than and just bigger than a check the behaviour near horizontal asymptote: $\lim_{y \to \infty} f(x)$ and $\lim_{y \to \infty} f(x)$ to find which side of the horizontal asymptotes you're on when far out to left or right.
 Easiest Method: You don't have to find the limit here, you can just use the other
 features of the graph that you already have to help you
 ther: You can NEVER cross a vertical asymptote, but can cross a horizontal one centrally.

We cannot cross a horizontal one far out though

Differentiation Turning/Stationary Solve $\frac{1}{dx} = 0$ Remember to include values where derivative is undefined too i.e. the holes (Max/Min/Extrema) the noies Absolute: check endpoint values too. Plug all x values into function and see which gives greatest value $\|\mathbf{f}\frac{dv}{dx^2}>0 \text{ min and }\frac{d^3y}{dx^2}<0 \text{ max}$ Or can do sign change test for $\frac{dy}{dx}$ When doesn't derivativ not exist? Discontinuities $f(x) = \begin{cases} 1, x \geq 0 \\ -1, x < 0 \end{cases}$ solve $\frac{d^2y}{dx^2} = 0$ Increasing: solve $\frac{dy}{dx} > 0$ decreasing: solve $\frac{dy}{dx} < 0$ Points of Inflection Increasing/Decreasing Convex/Concave concave up/convex; solve $\frac{d^2y}{d} > 0$ concave down/concave: solve $\frac{d^2y}{dx^2} < 0$ • Generally: $\frac{dy}{dx} = f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{f(x+h) - f(a)}$ • At a point a: $f'(a) = \lim_{h \to 0} \frac{f(x+h) - f(a)}{h}$ Alternate form: $f'(a) = \lim_{h \to 0} \frac{h}{f(x) - f(a)}$ (we don't really use this)

• To show derivative exists: show 2 sides limits equal $\lim_{h \to \infty} \frac{f(a+h) - f(a)}{h} \lim_{h \to \infty} \frac{f(a+h) - f(a)}{h}$ Differentiability \Rightarrow Continuity
Continuity \Rightarrow Differentiability $\frac{dy}{dx} = \frac{dy}{dx} = \frac{dy}{dx} = \frac{dy}{dx}$ $y = g(u), u = f(x) \Rightarrow \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$ Chain Rule Product Rule $y = uv \Rightarrow \frac{dy}{dx} = u\frac{dv}{dx} + v\frac{du}{dx}$ Quotient rule $y = \frac{u}{v} \Longrightarrow \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$ "every time we differentiate a y we write dy Implicit $\begin{aligned} &\ln(f(x)) \Rightarrow_{i=0}^{not} \\ &\sin f(x) \Rightarrow f'(x) \cos f(x) \\ &\cos f(x) \Rightarrow -f'(x) \sin f(x) \\ &e^{i(x)} \Rightarrow f'(x) e^{i(x)} \\ &e^{i(x)} \Rightarrow f'(x) e^{i(x)} \\ &e^{i(x)} \Rightarrow f'(x) e^{i(x)} \\ &\sin f(x) \Rightarrow f'(x) \sec^{i}(x) \tan f(x) \\ &\cot f(x) \Rightarrow -f'(x) \csc^{i}(x) \\ &\sin^{-1}(x) \Rightarrow f'(x) e^{i(x)} \\ &\sin^{-1}(x) \Rightarrow f'(x) e^{i(x)} \end{aligned}$ • $\cos^{-1} f(x) \Rightarrow -\frac{f'(x)}{\int_{1-f(x)}^{f'(x)}}$ • $\tan^{-1} f(x)) \Rightarrow \frac{f'(x)}{1+(f(x))^2}$ • $\sec^{-1} f(x) \Rightarrow \frac{f'(x)}{f(x)\sqrt{(f(x))^2}}$ • $cosec^{-1} f(x) \Rightarrow -\frac{f'(x)}{f(x)\sqrt{(f(x))^2-1}}$ • $\cot^{-1}f(x) = \frac{f(x)}{11/(6x)}$ If it is continuous over $\{a,b\}$ and wit is a number between $\{a\}$ and $\{b\}$ if it is continuous over $\{a,b\}$ at $\{a,b\}$ and $\{a,b\}$ at $\{a,b\}$ at $\{a,b\}$ and $\{a,b\}$ at $\{a,b\}$ at $\{a,b\}$ and $\{a,b\}$ at $\{a,b\}$ and $\{a,$ IVT MVT $y - y_1 = m(x - x_1)$ Differentiate to get m (tangent ||, Normal \perp) Tangents and Norm Local linear approx This is basically just asking for the tangent line curve & x axis: $\int_{x=a}^{x=b} y \, dx$ curve & y axis: $\int_{y=a}^{y=b} x \, dy$ Between 2 curves: $\int_{x=a}^{x=b} (\text{top curve-bottom curve}) dx$ Remember to split up if separate areas Properties Can swap limits: $\int_{a}^{b} x f(x) dx = -\int_{b}^{a} (x) dx$ Can split up: $\int_a^b (x) dx = \int_a^c (x) dx + \int_c^b (x) dx$ $\int x^{n} dx = \frac{x^{n+1}}{n+1} + c, n \neq -1$ $\int \frac{1}{kx} dx = \frac{1}{k} \ln|x| + c$ $\int \sin kx \, dx = -\frac{1}{\nu} \cos kx + c$ Integrals $\int_{\frac{\pi}{2}}^{\pi} \frac{1}{\sin(x)} \frac{1}{x} dx = \frac{\pi}{2} \cos kx + c$ $\int \cos kx \, dx = \frac{\pi}{2} \sin kx + c$ $\int e^{kx} \, dx = \frac{\pi}{2} e^{kx} + c$ $\int e^{kx} \, dx = \frac{\pi}{2} \sin kx + c$ $\int e^{kx} \, dx = \frac{\pi}{2} \tan kx + c$ $\int \sec^{2} kx \, dx = \frac{\pi}{2} \tan kx + c$ $\int \csc^{2} kx \, dx = \frac{\pi}{2} \cot kx + c$ $\int \csc kx \, dx = \frac{\pi}{2} \sin |\sec kx + \tan kx| + c$ $\int \csc kx \, dx = \frac{\pi}{2} \sin |\sec kx + \tan kx| + c$ $\int \csc kx \, dx = \frac{\pi}{2} \sin |\csc kx + \cot kx| + c$ $\int \frac{\pi}{\sqrt{x^{2} - \cos^{2}}} \, dx = \frac{\pi}{2} \sin^{-3} \left(\frac{x^{2}}{x^{2}}\right) + c$ $\int \frac{\pi}{\sqrt{x^{2} - \cos^{2}}} \, dx = \frac{\pi}{2} \cos^{-1} \left(\frac{x^{2}}{x^{2}}\right) + c$ $\int \frac{\pi}{\sqrt{x^{2} - \cos^{2}}} \, dx = \frac{\pi}{2} \sin^{-3} \left(\frac{x^{2}}{x^{2}}\right) + c$ $\int \frac{\pi}{\sqrt{x^{2} - \cos^{2}}} \, dx = \frac{\pi}{2} \sin^{-3} \left(\frac{x^{2}}{x^{2}}\right) + c$ $\int \frac{\pi}{\sqrt{x^{2} - \cos^{2}}} \, dx = \frac{\pi}{2} \sin^{-3} \left(\frac{x^{2}}{x^{2}}\right) + c$ $\int \frac{\pi}{\sqrt{x^{2} - \cos^{2}}} \, dx = \frac{\pi}{2} \sin^{-3} \left(\frac{x^{2}}{x^{2}}\right) + c$ Trapezium Rule $\frac{h}{2}[y_0 + 2(y_{1+}y_{2+}y_{3+}y_4 + \cdots) + y_n] h = \frac{b-a}{number\ of\ strips}$ Left: $h[y_0 + y_1 + y_2 + y_3 + \cdots y_{n-1}]$ $h = \frac{b-a}{number\ of\ strips}$ Right: $h[y_1 + y_2 + y_1 + y_4 + \cdots y_n]$ Midpoint: $h[y_{\frac{1}{2}} + y_{\frac{1}{2}} + y_{\frac{1}{2}} + \cdots + y_{n-\frac{2}{2}} + y_{n-\frac{1}{2}}]$ Kinematics: Distance= $\int_{t}^{t_2} |v(t)| dt$, Displacement= $\int_{t}^{t_2} v(t) dt$ Distances J_{i_1} : y(t) dt, Displacements J_{i_2} : y(t) dt Velocity. $\int_{t_1}^{t_2} a(t) dt$ or $\frac{ds}{dt}$ Acceleration $= \frac{ds}{dt} = \frac{d^2s}{dt^2}$ Changed direction: v = 0, Mowing right/up $\Rightarrow v > 0$ Mowing right/up $\Rightarrow v > 0$ Speeding up/velocity increasing/accel: a, v same sign Speeding up/velocity increasing/accel: a, v same sign S Slowing down/velocity decreasing/dec: a, v opp sign Max displacement/max distance from/furthest left or right or up or down: =v=0Arc length Volume of revolution Disc: $V = \pi \int_{x^{-2}}^{x-2} (radius)^2 dx$ y axis: $V = \pi \int_{y^{-2}}^{y-2} (radius)^2 dy$ Washer: $V = \pi \int_{x^{-2}}^{x-2} (outer radius)^2 - (inner radius)^2)]dx$ Note: $V = \pi \int_{v=a}^{y=b} [(outer radius)^2 - (inner radius)^2)] dy$ Volume of cross sections $\int_{a}^{b} A(x)dx \text{ where } A(x) =$ (\pm to x axis) cross secitonal area of the shape
Get y's on one side and x's on other and integrate each side
Remember: we only × and+ to re-arrange Differential equations Starting value $+ \int_{t_{-}}^{t_{2}} rate \ in - \int_{t_{-}}^{t_{2}} rate \ out$ Total Amount First : $\int_a^b f(x)dx = F(b) - F(a)$ i.e. $\int_a^b f'(x) = f(b) - f(a)$ Second: $\frac{d}{dx} \int_{a}^{x} f(t)dt = f(x)$

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